STOR 664 Homework 1, Fall 2022

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Due: Thursday August 25

These assignments use the NEW versions of the Amherst and Mount Airy/Charleston datasets, available on

http://rls.sites.oasis.unc.edu/faculty/rs/source/Data/amh1.csv

and

http://rls.sites.oasis.unc.edu/faculty/rs/source/Data/mta1.csv

Theory Part. Well, not really "theory" in the sense or proving new mathematical results, but I'd like you to work through these parts directly, evaluating \bar{x} , \bar{y} , $\sum (y_i - \bar{y})^2$, $\sum (x_i - \bar{x})(y_i - \bar{y})$, etc. in order to calculate $\hat{\beta}_0$, $\hat{\beta}_1$, the residual variance s^2 , etc., using the direct formulas given in the text rather than by using the regression commands in R or any other language (it's fine if you use R or Excel as a calculator to evaluate these numerical quantities quickly).

In each case assume the model

$$y_i = \beta_0 + \beta_1 (x_i - \bar{x}) + \epsilon_i$$

where the ϵ_i satisfy either of the assumptions (a) or (b) in the text.

- 1. For the Amherst data, find (a) $\hat{\beta}_0$ and $\hat{\beta}_1$, (b) the residual variance estimator s^2 , (c) the standard errors of $\hat{\beta}_0$ and $\hat{\beta}_1$, (d) formally test H_0 : $\beta_1 = 0$ against the alternative H_0 : $\beta_1 \neq 0$. Assume the x variable is Year, the y variable is annual mean temperature in Amherst, and that the standard assumptions are correct.
- 2. For the Mount Airy/Charleston data, find (a) $\hat{\beta}_0$ and $\hat{\beta}_1$, (b) the residual variance estimator s^2 , (c) the standard errors of $\hat{\beta}_0$ and $\hat{\beta}_1$, (d) formally test H_0 : $\beta_1 = 0$ against the alternative H_0 : $\beta_1 \neq 0$. Assume the x variable is summer mean temperature in Mount Airy, the y variable is summer mean temperature in Charleston, and that the standard assumptions are correct.

R Part. Now repeat the same calculations in R, using the 1m command. Typical commands will be of the form

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lm(y~x)
summary(lm(y~x))
# or
summary(lm(y~x1+x2)) # if there are two covariates x1 and x2
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after defining the variables x and y.

- 3. For the Amherst data, verify the results of part 1 and extend also to the model in which Year² is used as a covariate as well as Year. (Hint: you may want to rescale first, e.g. replace Year by Year/1000.) Draw a scatterplot of temperature against year, and show both fitted curves on the plot (you may find the lm(...)\$fitted command useful for this). What do you conclude about the possibility that the trend may be nonlinear?
- 4. For the Mount Airy/Charleston data, verify the results of part 2. Also consider (separately for Mount Airy and Charleston) whether there appears to be a time trend against Year, and state your conclusions from that.